

# New Exercises

to the book

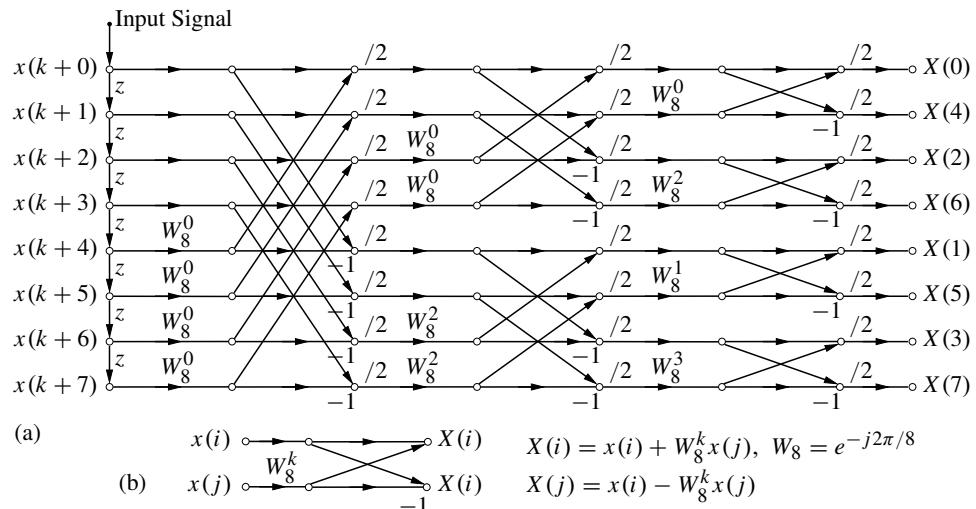
## Quantization Noise

by Bernard Widrow and István Kollár

<http://www.mit.bme.hu/books/quantization/>

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- 15.16** Following the lines of Subsection 15.7.3 in the Corrigenda, determine a formula similar to (15.26b) accounting for the roundoff error of the complex coefficients  $W_N$ , using the same value of  $q$  for their storage as for the signal. Assume that the input is white noise.
- 15.17** Repeat the calculations given in Subsection 15.7.3 in the Corrigenda, to determine a formula similar to (15.26b) for a downscaled scheme: after each addition/subtraction, before storage (quantization) the samples are divided by 2. See Fig. 15.17.1.



**Figure 15.17.1** DIT FFT scheme with downscalings by 2

- 15.18** Verify the results of Exercise 15.17 by computer simulation, for  $B = 32$ ,  $N = 256$ , uniformly distributed random numbers in  $(-1, 1)$ . Make a “fair” comparison with the results of Exercise 15.6.
- 15.19** Repeat Exercise 15.16 for the downscaled scheme given in Fig. 15.17.1: after each addition/subtraction, before storage (quantization) the samples are divided by 2. See Fig. 15.17.1.
- 15.20** Verify the results of Exercise 15.19 by computer simulation, for  $B = 32$ ,  $N = 256$ , uniformly distributed random numbers in  $(-1, 1)$ .

- 15.21** Determine a formula similar to (15.27), accounting for the roundoff error of the complex coefficients  $W_N$  in the DFT, assuming the same value of  $q$  for their storage as for the signal. Assume that the input is white noise, uniform in  $(-1/32, 1/32)$ ,  $B = 16$ , numbers in  $(-1, 1)$ ,  $N = 256$ . Compare it to (15.27).
- 15.22** Assume that the input signal is represented on 12 bits: 10 integer bits, and two fractional bits. Assume that in the FFT, 16-bit integer arithmetic is used. Determine the variance of the roundoff error calculated for  $X(k)$ , due to input roundoff. Is this different from the effect of input roundoff in a DFT?
- 15.23** Following the lines of Subsection 15.7.3 in the Corrigenda, determine the formula equivalent to (15.26b) for the case of decimation-in-frequency (DIF) FFT (see Fig. 15.23.1). Is this bound different from the one obtained for DIT FFT? Why?

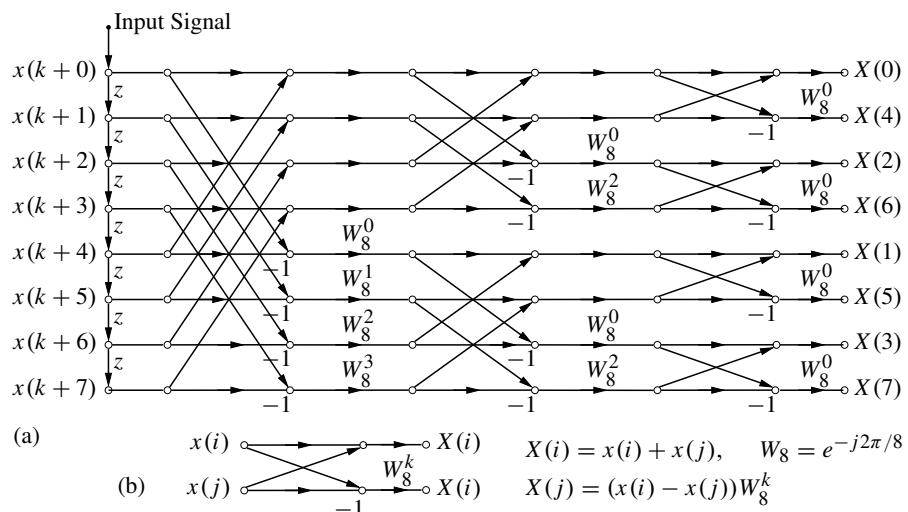


Figure 15.23.1 DIF FFT scheme

- 15.24** Verify the formula obtained in Exercise 15.23 by computer simulation.

**19.39** Prove that

- (a) among all zero-order dithers with zero mean, the dither uniformly distributed in  $\pm q/2$  has the smallest variance,
- (b) among all first-order dithers with zero mean, the dither triangularly distributed in  $\pm q$  has the smallest variance.